# Programming Languages: Type Systems

Onur Tolga Şehitoğlu

Computer Engineering, METU

20 March 2008

- 1 Type Systems
- 2 Polymorphism
  - Inclusion Polymorphism
  - Parametric Polymorphism
- 3 Overloading
- 4 Coercion
- 5 Type Inference

#### Type Systems

#### Design choices for types:

- monomorphic vs polymorphic type system.
- overloading allowed?
- coercion(auto type conversion) applied, how?
- type relations and subtypes exist?

# Polymorphism

- Monomorphic types: Each value has a single specific type. Functions operate on a single type. C and most languages are monomorphic.
- Polymorphism: A type system allowing different data types handled in a uniform interface:
  - Ad-hoc polymorphism: Also called overloading. Functions that can be applied to different types and behave differently.
  - 2 Inclusion polymorphism: Polymorphism based on subtyping relation. Function applies to a type and all subtypes of the type (class and all subclasses).
  - 3 Parametric polymorphism: Functions that are general and can operate identically on different types

# Subtyping

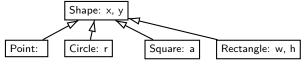
- C types: char ⊆ short ⊆ int ⊆ long
- Need to define arithmetic operators on them separately?
- Consider all strings, alphanumeric strings, all strings from small letters, all strings from decimal digits. Ned to define special concatenation on those types?
- $\bullet$   $f: T \to V$ ,  $U \subseteq T \Rightarrow f: U \to V$
- Most languages have arithmetic operators operating on different precisions of numerical values.

#### Inheritance

```
struct Point { int x, y; };
struct Circle { int x, y, r; };
struct Square { int x, y, a; };
struct Rectangle { int x, y, w, h; };

void move (Point p, int nx, int ny) {
    p.x=nx; p.y=ny;}
```

Moving a circle or any other shape is too different?

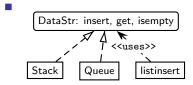


#### Haskell extensible records:

```
import Hugs. Trex; -- Only in -98 mode!!!
type Shape = Rec (x::Int, y::Int)
type Circle = Rec (x::Int, y::Int, r::Int)
type Square = Rec (x::Int, y::Int, w::Int)
type Rectangle = Rec (x::Int, y::Int, w::Int, h::Int)
move (x=_,y=_|rest) b c = (x=b,y=c|rest)
(a::Shape)=(x=12, y=24)
(b:: Circle) = (x=12, y=24, r=10)
(c::Square)=(x=12,y=24,w=4)
(d::Rectangle) = (x=12, y=24, w=10, h=5)
Main > move b 4 5
(r = 10, x = 4, y = 5)
Main > move c 4 5
(w = 4, x = 4, y = 5)
Main > move d 4 5
(h = 5, w = 10, x = 4, y = 5)
```

#### Haskell Classes

- Subtyping hierarchy based on classes
- An instance implements interface functions of the class
- Functions operating on classes (using interface functions) can be defined



listinsert :: DataStr  $a \Rightarrow (a \ v) \rightarrow [v] \rightarrow (a \ v)$ 

Called interface in OO programming

```
class DataStr a where
    insert :: (a v) -> v -> (a v)
    get :: (a \ v) \rightarrow Maybe (v,(a \ v))
    isempty :: (a v) -> Bool
instance DataStr Stack where
    insert \times v = push v \times v
    get x = pop x
    isempty Empty = True
    isemptv _ = False
instance DataStr Queue where
    insert \times v = enqueue v \times
    get x = dequeue x
    isempty EmptyQ = True
    isemptv _ = False
insertlist :: DataStr a => (a v) -> [v] -> (a v)
insertlist \times \Pi = \times
insertlist x (el:rest) = insertlist (insert x el) rest
data Stack a = Empty | St [a] deriving Show
data Queue a = EmptyQ | Qu [a] deriving Show
```

# Parametric Polymorphism

- Polymorphic types: A value can have multiple types.
   Functions operate on multiple types uniformly
- identity x = x function. type:  $\alpha \to \alpha$  identity 4: 4, identity "ali": "ali", identity (5,"abc"): (5,"abc") int  $\to$  int,  $String \to String$ , int  $\times String \to int \times String$
- compose f g x = f (g x) function type:  $(\beta \to \gamma) \to (\alpha \to \beta) \to \alpha \to \gamma$ compose square double 3: 36,  $(int \to int) \to (int \to int) \to int \to int.$ compose listsum reverse [1,2,3,4]: 10  $([int] \to int) \to ([int] \to [int]) \to [int] \to int$

- filter f [] = []

  filter f (x:r) = if (f x) then x:(filter f r) else (filter r)  $(\alpha \to Bool) \to [\alpha] \to [\alpha]$ filter ((<) 3) [1,2,3,4,5,6] : [4,5,6]  $(int \to Bool) \to [int] \to [int]$ filter identity [True, False, True, False] :

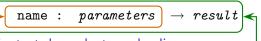
  [True,True]  $(Bool \to Bool) \to [Bool] \to [Bool]$
- Operations are same, types are different.
- Types with type variables: polytypes
- Most functional languages are polymorphic
- Object oriented languages provide polymorphism through inheritance

### Overloading

- Overloading: Using same identifier for multiple places in same scope
- Example: Two different functions, two distinct types, same name.
- Polymorphic function: one function that can process multiple types.
- C++ allows overloading of functions and operators.

```
typedef struct Comp { double x, y; } Complex;
double mult(double a, double b) { return a*b; }
Complex mult(Complex s, Complex u) {
    Complex t;
    t.x = s.x*u.x - s.y*u.y;
    t.y = s.x*u.y + s.y*u.x;
    return t;
}
Complex a,b; double x,y; ...; a=mult(a,b); x=mult(y,2.1);
```

- Binding is more complicated. not only according to name but according to name and type
- Function type:



- Context dependent overloading—:

  Overloading based on function name, parameter type and return type.
- Context independent overloading: Overloading based on function name and parameter type. No return type!

## Context dependent overloading

Which type does the expression calling the function expects (context)?

```
int f(double a) { ....① }
int f(int a) { ....② }
double f(int a) { ....③ }
double x,y;
int a,b;
```

```
a=f(x); (1)(x double)
a=f(a); (2)(a int, assign int)
x=f(a); (3)(a int, assign double)
x=2.4+f(a); (3)(a int, mult double)
a=f(f(x)); (2)(1)(x double, f(x):int, assign int)
a=f(f(a)); (2)(2) or (1)(3)???
```

Problem gets more complicated. (even forget about coercion)

# Context independent overloading

- Context dependent overloading is more expensive.
- Complex and confusing. Useful as much?
- Most overloading languages are context independent.
- Context independent overloading forbids ② and ③ functions defined together.
- "name: parameters" part should be unique in "name: parameters → result", in the same scope
- Overloading is not much useful. So languages avoid it.

#### Use carefully:

Overloading is useful only for functions doing same operations. Two functions with different purposes should not be given same names. Confuses programmer and causes errors

Is variable overloading possible? What about same name for two types?

#### Coercion

Making implicit type conversion for ease of programming.

- $\blacksquare$  Are other type of coercions are possible? (like A \*  $\to$  A, A  $\to$  A \* ). Useful?
- May cause programming errors: x=k=3.25 : x becomes 3.0
- Coercion + Overloading: too complex.
- Most newer languages quit coercion completely (Strict type checking)

## Type Inference

- Type system may force user to declare all types (C and most compiled imperative languages), or
- Language processor infers types. How?
- Each expression position provide information (put a constraint) on type inference:
  - Equality  $e = x, x :: \alpha, y :: \beta \Rightarrow \alpha \equiv \beta$
  - Expressions  $e = a + f \times + :: Num \rightarrow Num \rightarrow Num \rightarrow a :: Num, f :: <math>\alpha \rightarrow Num, e :: Num$
  - Function application  $e = f \times \Rightarrow e :: \beta, x :: \alpha, f :: (\alpha \rightarrow \beta)$
  - Type constructors  $f(x:r) = t \Rightarrow x :: \alpha, t :: \beta, f :: ([\alpha] \rightarrow \beta)$
- Inference of all values start from the most general type (i.e. any type  $\alpha$ )
- Type inference finds the most general type satisfying the constraints.